

### Reading 6: Time Value of Money

#### 1. Interest Rate ( $i$ )

- $i = R_f + \text{Inf P} + \text{Default Risk P} + \text{Liquidity P} + \text{Maturity P}$
- Nominal  $R_f$   $i$  rate = Real  $R_f$   $i$  Rate + Inf P
- $i$  rate as a growth rate =  $g = \left(\frac{FV_N}{PV}\right)^{\frac{1}{N}} - 1$

#### 2. PV and FV of CF =

- $PV = \frac{FV}{(1+r)^N}$
- PV of Perpetuity =  $\frac{PMT}{r}$
- PV (for more than one Compounding per year) =  $PV = FV_N \left(1 + \frac{r_s}{m}\right)^{-m \times N}$   
where  $r_s = \text{stated ann } i - \text{rate}$
- $FV_N = PV(1+r)^N$
- FV (for more than one Compounding per year) =  $FV_N = \left(1 + \frac{r_s}{m}\right)^{m \times N}$
- FV (for Continuous Compounding) =  $FV_N = PV e^{r_s \times N}$
- Solving for  $N = \frac{LN\left(\frac{FV}{PV}\right)}{LN(1+r)}$  (where LN = natural log)

#### 4. Stated & Effective Rates

- Periodic  $i$  Rate =  $\frac{\text{Stated Ann } i \text{ Rate}}{\text{No of Compounding Periods in One Year}}$
- Effective (or Equivalent) Ann Rate (EAR = EFF%) =  $(1 + \text{Periodic } i \text{ Rate})^m - 1$

- EAR (with Continuous Compounding) = EAR =  $e^{r_s} - 1$

#### 5. PV & FV of Ordinary Annuity

- $PV_{OA} = \sum_{t=1}^n \frac{PMT}{(1+r)^t} = PMT \left[ \frac{1 - \frac{1}{(1+r)^N}}{r} \right]$
- $FV_{OA} = \sum_{t=1}^n (PMT_t (1+r))^{N-t} = PMT \left[ \frac{(1+r)^N - 1}{r} \right]$
- Size of Annuity Payment =  $PMT = \frac{PV}{PV \text{ of Annuity Factor}}$
- PV of Annuity Factor =  $\frac{1 - \frac{1}{\left[1 + \left(\frac{r_s}{m}\right)^{m \times N}\right]}}{\frac{r_s}{m}}$

#### 6. PV & FV of Annuity Due

- $PV_{AD} = PMT \left[ \frac{1 - \frac{1}{(1+r)^N}}{r} \right] + PMT$  at  $t = 0$   
 $PV_{OA} + PMT$
- $FV_{AD} = PMT \left[ \frac{(1+r)^N - 1}{r} \right] (1+r) = FV_{OA} \times (1+r)$

### Reading 7: Discounted Cash Flow Applications

$$1. NPV = \sum_{t=1}^n \frac{CF_t}{(1+r)^t} - cf_0$$

#### 2. IRR (when project's CFs are perpetuity) =

$$NPV = -I_0 + \frac{\overline{CF}}{IRR} = 0$$

$$3. HPR = \frac{(P_1 - P_0 + D_1)}{P_0}$$

$$4. MMWR = \sum_{t=0}^T \frac{CF}{(1+IRR)^t} = 0 \text{ (IRR represents the MWR)}$$

#### 5. TWR:

- TWR (when no external CF) =  $r_{TWR} = HPR = r_t = \frac{MV_1 - MV_0}{MV_0}$
- TWR (for more than one periods) =  $r_{TWR} = [(1+r_{t,1}) \times (1+r_{t,2}) \times \dots \times (1+r_{t,n})] - 1$
- Annualized TWR (when investment is for more than one year) =  $[(1 + R_1)(1 + R_2 \dots + (1 + R_n))]^{\frac{1}{n}} - 1$
- TWR (for the year) =  $r_{TWR} = [(1+R_1) \times (1+R_2) \times \dots \times (1+R_{365})] - 1$  where  $R_1 = \frac{MV_1 - MV_0}{MV_0}$

#### 6. Bank Discount Yield = BDY = $r_{BD} =$

$$\frac{360}{n} \frac{\text{Par} - \text{Price}}{\text{Par}} \text{ therefore Price} = \text{Par} \left(1 - \frac{n \times r_{BD}}{360}\right)$$

$$7. \text{Holding Period Yield} = HPY = \frac{(P_1 - P_0 + D_1)}{P_0}$$

$$8. \text{Effective Annual Yield} = EAY = (1 + HPY)^{365/t} - 1 \text{ (Rule: EAY} > \text{BDY)}$$

#### 9. Money Market Yield (or CD equivalent Yield) $r_{MM}$ :

- $r_{MM} = HPY \times \left(\frac{360}{t}\right)$
- $r_{MM} = (r_{BD}) \times \frac{\text{Face Value of the Treasury Bill}}{\text{Purchase Price}}$

- $r_{MM} = \frac{360(r_{BD})}{360 - (t)(r_{BD})}$  (Rule:  $r_{MM} > r_{BD}$ )

10. Bond Equivalent Yield =  $BDY =$   
Semiannual Yield  $\times 2$

### Reading 8: Statistical Concepts & Market Returns

1. Range = Max Value – Min Value

2. Class Interval =  $i \geq \frac{H-L}{k}$  where

- $i$  = class interval
- $H$  = highest value
- $L$  = lowest value,  $k$  = No. of classes.

3. Absolute Frequency = Actual No of Observations (obvs) in a given class interval

4. Relative Frequency =  $\frac{\text{Absolute Frequency}}{\text{Total No of Obvs}}$

5. Cumulative Absolute Frequency = Add up the Absolute Frequencies

6. Cumulative Relative Frequency = Add up the Relative Frequencies

7. Arithmetic Mean =  $\frac{\text{Sum of obvs in database}}{\text{No. of obvs in the database}}$

8. Median = Middle No (when observations are arranged in ascending/descending order)

- For Even no of obvs locate median at  $\frac{n}{2}$

- For Odd no. of obvs locate median at  $\frac{n+1}{2}$

9. Mode = obvs that occurs most frequently in the distribution

10. Weighted Mean =  $\bar{X}_w = \frac{\sum_{i=1}^n w_i X_i}{(w_1 X_1 + w_2 X_2 + \dots + w_n X_n)}$

11. Geometric Mean =  $GM = \sqrt[n]{X_1 X_2 \dots X_n}$   
with  $X_i \geq 0$  for  $i = 1, 2, \dots, n$ .

12. Harmonic Mean =  $H.M = \bar{X}_H = \frac{n}{\sum_{i=1}^n \left(\frac{1}{X_i}\right)}$

13. Population Mean =  $\mu = \frac{\sum_{i=1}^n X_i}{N}$  with  $X_i > 0$   
for  $i = 1, 2, \dots, n$ .

14. Sample Mean =  $\bar{X} = \frac{\sum_{i=1}^n X_i}{n}$  where  $n =$   
number of observation in the sample

15. Measures of Location:

- Quartiles =  $\frac{\text{Distribution}}{4}$
- Quintiles =  $\frac{\text{Distribution}}{5}$
- Deciles =  $\frac{\text{Distribution}}{10}$ ,
- Percentiles =  $L_y = (n + 1) \frac{y}{100}$

16. Mean Absolute Deviation =  $MAD = \frac{\sum_{i=1}^n |X_i - \bar{X}|}{n}$

17. Population Var =  $\sigma^2 = \frac{\sum_{i=1}^N (X_i - \mu)^2}{N}$

18. Population S.D =  $\sqrt{\sigma^2} = \sqrt{\frac{\sum_{i=1}^N (X_i - \mu)^2}{N}}$

19. Sample Var =  $s^2 = \frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n-1}$

20. Sample S.D =  $s = \sqrt{\frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n-1}}$

21. Semi-var =  $\sum_{\text{For all } X_i \leq \bar{X}} \frac{(X_i - \bar{X})^2}{n-1}$

22. Semi-deviation (Semi S.D) =

$$\sqrt{\text{semivariance}} = \sqrt{\sum_{\text{For all } X_i \leq \bar{X}} \frac{(X_i - \bar{X})^2}{n-1}}$$

23. Target Semi-var =  $\sum_{\text{For all } X_i \leq B} \frac{(X_i - B)^2}{n-1}$   
where  $B =$  Target Value

24. Target Semi-Deviation =  $\sqrt{\text{target semivariance}} = \sqrt{\sum_{\text{For all } X_i \leq B} \frac{(X_i - B)^2}{n-1}}$

25. Coefficient of Variation =  $CV = \left(\frac{S}{\bar{X}}\right)$   
where  $s =$  sample S.D and  $\bar{X} =$  sample mean

26. Sharpe Ratio =  $\frac{\text{Mean Portfolio } R - \text{Mean } R_f}{S.D \text{ of Portfolio } R}$

27. Excess Kurtosis = Kurtosis – 3

28. Geometric Mean  $R \approx$   
 Arithmetic Mean  $R - \frac{\text{Variance of } R}{2}$

### Reading 9: Probability Concepts

1. Empirical Prob of an event  $E = P(E) = \frac{\text{Prob of event } E}{\text{Total Prob}}$

2. Odds for event  $E = \frac{\text{Prob of } E}{1 - \text{Prob of } E}$

3. Odds against event  $E = \frac{1 - \text{Prob of } E}{\text{Prob of } E}$

4. Conditional Prob of A given that B has occurred =  $P(A|B) = \frac{P(AB)}{P(B)} \rightarrow P(B) \neq 0$ .

5. Multiplication Rule (Joint probability that both events will happen):

$$P(A \text{ and } B) = P(AB) = P(A|B) \times P(B)$$

$$P(B \text{ and } A) = P(BA) = P(B|A) \times P(A)$$

6. Addition Rule (Prob that event A or B will occur):

$$P(A \text{ or } B) = P(A) + P(B) - P(AB)$$

$$P(A \text{ or } B) = P(A) + P(B) \text{ (when events are mutually exclusive because } P(AB) = 0)$$

7. Independent Events:

- Two events are independent if:  $P(B|A) = P(B)$  or if  $P(A|B) = P(A)$

- Multiplication Rule for two independent events =  $P(A \& B) = P(AB) = P(A) \times P(B)$
- Multiplication Rule for three independent events =  $P(A \text{ and } B \text{ and } C) = P(ABC) = P(A) \times P(B) \times P(C)$

8. Complement Rule (for an event  $S$ ) =  $P(S) + P(S^c) = 1$  (where  $S^c$  is the event not  $S$ )

9. Total Probability Rule:

$$P(A) = P(AS) + P(AS^c) = P(A|S) \times P(S) + P(A|S^c) \times P(S^c)$$

$$P(A) = P(AS_1) + P(AS_2) + \dots + P(AS_n) = P(A|S_1) \times P(S_1) + P(A|S_2) \times P(S_2) \dots P(A|S_n) \times P(S_n)$$

(where  $S_1, S_2, \dots, S_n$  are mutually exclusive and exhaustive scenarios)

10. Expected  $R = E(w_i R_i) = w_i E(R_i)$

11.  $\text{Cov}(R_i, R_j) = \sum_{i=1}^n (p(R_i - ER_i))(R_j - ER_j)$

$$\text{Cov}(R_i, R_j) = \text{Cov}(R_j, R_i)$$

$$\text{Cov}(R, R) = \sigma^2(R)$$

12. Portfolio Var =  $\sigma^2(R_p) =$

$$\sum_{i=1}^n \sum_{j=1}^n w_i w_j \text{Cov}(R_i, R_j)$$

$$\sigma^2(R_p) = w_1^2 \sigma^2(R_1) + w_2^2 \sigma^2(R_2) + w_3^2 \sigma^2(R_3) + 2w_1 w_2 \text{Cov}(R_1, R_2) + 2w_1 w_3 \text{Cov}(R_1, R_3) + 2w_2 w_3 \text{Cov}(R_2, R_3)$$

13. Standard Deviation (S.D) =  $\sqrt{w_1^2 R_1 + w_2^2 R_2 + w_3^2 R_3}$

14. Correlation (b/w two random variables  $R_i, R_j$ ) =  $\rho(R_i, R_j) = \frac{\text{Cov}(R_i, R_j)}{\sigma_{R_i} \times \sigma_{R_j}}$

15. Bayes' Formula =  $P(\text{Event} | \text{New Information}) = \frac{P(\text{New Information} | \text{Event})}{P(\text{New Information})} \times P(\text{Prior prob. of Event})$

16. Multiplication Rule of Counting =  $n$  factorial =  $n! = n(n-1)(n-2)(n-3) \dots 1$ .

17. Multinomial Formula (General formula for labeling problem) =  $\frac{n!}{n_1! n_2! \dots n_k!}$

18. Combination Formula (Binomial Formula) =  ${}^n C_r = \binom{n}{r} = \frac{n!}{(n-r)! r!}$

where  $n$  = total no. of objects and  $r$  = no. of objects selected.

19. Permutation =  ${}^n P_r = \frac{n!}{(n-r)!}$

### Reading 10: Common Probability Distributions

1. Probability Function (for a binomial random variable)  $p(x) = p(X=x) = \binom{n}{x} p^x (1-p)^{n-x} = \frac{n!}{(n-x)! x! p^x} (1-p)^{n-x}$  (for  $x = 0, 1, 2, \dots, n$ )

- $x$  = success out of  $n$  trials
  - $n-x$  = failures out of  $n$  trials
  - $p$  = probability of success
  - $1-p$  = probability of failure
  - $n$  = no of trials.
2. Probability Density Function (pdf) =  $f(x)$   

$$= \begin{cases} \frac{1}{b-a} & \text{for } a \leq x \leq b \\ 0 & \text{otherwise} \end{cases}$$

$$F(x) = \frac{x-a}{b-a} \text{ for } a < x < b$$
3. Normal Density Funct =  $f(x) = \frac{1}{\sigma\sqrt{2\pi}} \exp\left(-\frac{(x-\mu)^2}{2\sigma^2}\right)$  for  $-\infty < x < +\infty$
4. Estimations by using Normal Distribution:
- Approximately 50% of all obsv fall in the interval  $\mu \pm \frac{2}{3}\sigma$
  - Approx 68% of all obsvs fall in the interval  $\mu \pm \sigma$
  - Approx 95% of all obsvs fall in the interval  $\mu \pm 2\sigma$
  - Approx 99% of all obsvs fall in the interval  $\mu \pm 3\sigma$
  - More precise intervals for 95% of the obsvs are  $\mu \pm 1.96\sigma$  and for 99% of the observations are  $\mu \pm 2.58\sigma$ .
5. Z-Score (how many S.Ds away from the mean the point  $x$  lies)  $z = \frac{\text{standard normal random variable} = \frac{X-\mu}{\sigma}}$  (when  $X$  is normally distributed)
6. Roy's Safety-Frist Criterion = SF Ratio =  $\frac{[E(R_P)-R_L]}{\sigma_P}$
7. Sharpe Ratio =  $\frac{[E(R_P)-R_f]}{\sigma_P}$
8. Value at Risk = VAR = Minimum \$ loss expected over a specified period at a specified prob level.
9. Mean ( $\mu_L$ ) of a lognormal random variable =  $\exp(\mu + 0.50\sigma^2)$
10. Variance ( $\sigma_L^2$ ) of a lognormal random variable =  $\exp(2\mu + \sigma^2) \times [\exp(\sigma^2) - 1]$ .
11. Log Normal Price =  $S_T = S_0 \exp(r_{0,T})$   
 Where,  $\exp = e$  and  $r_{0,t}$  = Continuously compounded return from 0 to  $T$
12. Price relative = End price / Beg price =  $S_{t+1} / S_t = 1 + R_{t,t+1}$   
*where,*  
 $R_{t,t+1}$  = holding period return on the stock from  $t$  to  $t + 1$ .
13. Continuously compounded return associated with a holding period from  $t$  to  $t + 1$ :  
 $r_{t,t+1} = \ln(1 + \text{holding period return})$  or  
 $r_{t,t+1} = \ln(\text{price relative}) = \ln(S_{t+1} / S_t) = \ln(1 + R_{t,t+1})$
14. Continuously compounded return associated with a holding period from 0 to  $T$ :  
 $R_{0,T} = \ln(S_T / S_0)$  or  $r_{0,T} = r_{T-1,T} + r_{T-2,T-1} + \dots + r_{0,1}$   
 Where,  
 $r_{T-1,T}$  = One-period continuously compounded returns
15. When one-period continuously compounded returns (i.e.  $r_{0,1}$ ) are IID random variables.  

$$E(r_{0,T}) = E(r_{T-1,T}) + E(r_{T-2,T-1}) + \dots + E(r_{0,1}) = \mu T$$
 And  

$$\text{Variance} = \sigma^2(r_{0,T}) = \sigma^2 T$$
  

$$\text{S.D.} = \sigma(r_{0,T}) = \sigma\sqrt{T}$$
16. Annualized volatility = sample S.D. of one period continuously compounded returns  $\times \sqrt{T}$

### Reading 11: Sampling and Estimation

1. Var of the distribution of the sample mean =  $\frac{\sigma^2}{n}$
2. S.D of the distribution of the sample mean =  $\sqrt{\frac{\sigma^2}{n}}$

3. Standard Error of the sample mean:
- When the population S.D ( $\sigma$ ) is known  
 $= \sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$
  - When the population S.D ( $\sigma$ ) is not known =  $s_{\bar{x}} = \frac{s}{\sqrt{n}}$  where  $s$  = sample S.D estimate of  $s = \frac{\sqrt{\text{sample variance}}}{\sqrt{s^2}}$  where  $s^2 = \frac{\sum_{i=1}^n (X_i - \bar{X})^2}{n-1}$
4. Finite Population Correction Factor = fpc  
 $= \sqrt{\frac{N-n}{N-1}}$  where  $N$  = population
5. New Adjusted Estimate of Standard Error  
 = (Old estimated standard error  $\times$  fpc)
6. Construction of Confidence Interval (CI) = Point estimate  $\pm$  (Reliability factor  $\times$  Standard error)
- CI for normally distributed population with known variance =  $\bar{x} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$
  - CI for normally distributed population with unknown variance =  $\bar{x} \pm z_{\alpha/2} \frac{s}{\sqrt{n}}$  where  $S$  = sample S.D.
7. Student's t distribution  
 $\mu = \bar{X} \pm t_{\alpha/2} \frac{s}{\sqrt{n}}$
8. Z-ratio =  $Z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$

$$9. \text{ t-ratio} = t = \frac{\bar{x} - \mu}{s / \sqrt{n}}$$

### Reading 12: Hypothesis Testing

1. Test Statistic =  $\frac{\text{Sample Statistic} - \text{Hypothesized Value of pop parameter}}{\text{standard error of sample statistic}^*}$

\*when Pop S.D is unknown, the standard error of sample statistic is give by  $S_{\bar{x}} = \frac{s}{\sqrt{n}}$

\*when Pop S.D is unknown, the standard error of sample statistic is give by  $\sigma_{\bar{x}} = \frac{\sigma}{\sqrt{n}}$

2. Power of Test = 1-Prob of Type II Error
3.  $z = \frac{\bar{x} - \mu_0}{\frac{\sigma}{\sqrt{n}}}$  (when sample size is large or small but pop S.D is known)
4.  $z = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$  (when sample size is large but pop S.D is unknown where  $s$  is sample S.D)
5.  $t_{n-1} = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}}$  (when sample size is large or small and pop S.D is unknown and pop sampled is normally or approximately normally distributed)

6. Test Statistic for a test of diff b/w two pop means (normally distributed, pop var unknown but assumed equal)

$$t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\left(\frac{S_p^2}{n_1} + \frac{S_p^2}{n_2}\right)^{1/2}} \text{ where } S_p^2 = \text{pooled estimator of common variance} = \frac{(n_1 - 1)S_1^2 + (n_2 - 1)S_2^2}{n_1 + n_2 - 2} \text{ where } df = n_1 + n_2 - 2.$$

7. Test Statistic for a test of diff b/wn two pop means (normally distributed, unequal and unknown pop var unknown)

$$t = \frac{(\bar{X}_1 - \bar{X}_2) - (\mu_1 - \mu_2)}{\left(\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}\right)^{1/2}} \text{ In this df calculated as } df = \frac{\left(\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}\right)^2}{\frac{S_1^2}{n_1} + \frac{S_2^2}{n_2}}$$

8. Test Statistic for a test of mean differences (normally distributed populations, unknown population variances)

- $t = \frac{\bar{d} - \mu_{d0}}{s_{\bar{d}}}$
- sample mean difference =  $\bar{d} = \frac{1}{n} \sum_{i=1}^n d_i$
- sample variance =  $S_{\bar{d}}^2 = \frac{\sum_{i=0}^n (d_i - \bar{d})^2}{n-1}$
- sample S.D =  $\sqrt{S_{\bar{d}}^2}$

- sample error of the sample mean difference =  $s \bar{d} = \frac{S_d}{\sqrt{n}}$
8. Chi Square Test Statistic (for test concerning the value of a normal population variance)  $X^2 = \frac{(n-1)S^2}{\sigma_0^2}$  where  $(n-1) = df$  and  $S^2 = \text{sample variance} = \frac{\sum_{i=0}^n (X_i - \bar{X})^2}{n-1}$
9. Chi Square Confidence Interval for variance  
Lower limit =  $L = \frac{(n-1)S^2}{\chi_{a/2}^2}$  and Upper limit =  $U = \frac{(n-1)S^2}{\chi_{1-a/2}^2}$
10. F-test (test concerning differences between variances of two normally distributed populations)  $F = \frac{S_1^2}{S_2^2}$   
 $S_1^2 = 1st \text{ sample var with } n_1 \text{ obs}$   $S_2^2 = 2nd \text{ sample var with } n_2 \text{ obs}$   
 $df_1 = n_1 - 1 \text{ numerator } df$   
 $df_2 = n_2 - 1 \text{ denominator } df$
11. Relation between Chi Square and F-distribution =  $F = \frac{\chi_1^2/m}{\chi_2^2/n}$  where:
- $X_1^2$  is one chi square random variable with one m degrees of freedom

- $X_2^2$  is another chi square random variable with one n degrees of freedom
12. Spearman Rank Correlation =  $r_s = 1 - \frac{6 \sum_{i=1}^n d_i^2}{n(n^2 - 1)}$
- For small samples rejection points for the test based on  $r_s$  are found using table.
  - For large sample size (e.g.  $n > 30$ ) t-test can be used to test the hypothesis i.e.  
 $t = \frac{(n-2)^{1/2} r_s}{(1-r_s^2)^{1/2}}$

### Reading 13: Technical Analysis

1. Relative Strength Analysis =  $\frac{\text{Price of asset}}{\text{Price of the Benchmark Asset}}$
2. Price Target for the
- Head and Shoulders = Neckline – (Head – Neckline)
  - Inverse Head and Shoulders = Neckline + (Neckline – Head)
3. Simple Moving Average =  $\frac{P_1 + P_2 + P_3 \dots + P_n}{N}$
4. Momentum Oscillator (or Rate of Change Oscillator ROC):
- Momentum Oscillator Value M =  $(V - V_x) \times 100$
- (where V = most recent closing price and  $V_x$  = closing price x days ago)
- Alternate Method to calculate M =  $\frac{V}{V_x} \times 100$
5. Relative Strength Index = RSI =  $100 - \frac{100}{1+RS}$  where  $RS = \frac{\sum(\text{Up changes})}{\sum(\text{Down changes})}$
6. Stochastic Oscillator (composed of two lines %K and %D):
- $\%K = 100 \left( \frac{C-L14}{H14-L14} \right)$  where: C = latest closing price, L14 = lowest price in last 14 days, H14 is highest price in last 14 days
  - $\%D$  = Average of the last three %K values calculated daily.
7. Put/Call Ratio (Type of Sentiment Indicators) =  $\frac{\text{Volume of Put Options Traded}}{\text{Volume of Call Options Traded}}$
8. Short Interest Ratio (Type of Sentiment Indicators) =  $\frac{\text{Short Interest}}{\text{Average Daily Trading Volume}}$
9. Arms Index TRIN i.e. Trading Index (Type of Flow of funds Indicator) =  $\text{Arm Index or TRIN} = \frac{\text{No. of Advan Issues} \div \text{No. of Declin Issues}}{\text{Volume of Advan Issues} \div \text{Volume of Declin Issues}}$

### Reading 14: Topics in Demand & Supply Analysis

$$1. Q^d_x = f(P_x, I, P_y)$$

$$\text{Price Elasticity of Demand} = E_{px}^d =$$

$$\frac{\% \Delta \text{ in Quantity Demanded}}{\% \Delta \text{ in Price}} = \frac{\frac{\Delta Qdx}{Qdx}}{\frac{\Delta Px}{Px}} = \left( \frac{\Delta Qdx}{Px} \right) \left( \frac{Px}{Qdx} \right)$$

$$2. \text{ Income Elasticity of Demand} = E_I^d =$$

$$\frac{\% \Delta \text{ in Quantity Demanded}}{\% \Delta \text{ in Income}} = \left( \frac{\Delta Qdx}{I} \right) \left( \frac{I}{Qdx} \right)$$

$$3. \text{ Cross Elasticity} = E_{py}^d =$$

$$\frac{\% \Delta \text{ in Quantity Demanded of Good X}}{\% \Delta \text{ in Price of Good Y}} = \left( \frac{\Delta Qdx}{Py} \right) \left( \frac{Py}{Qdx} \right)$$

$$4. \text{ Total cost of production} = TC = (w)(L) + (r)(K)$$

$$5. TR = (P)(Q)$$

$$6. MR = \Delta TR / \Delta Q$$

$$7. MR = \frac{(P)(\Delta Q)}{\Delta Q} + \frac{(Q)(\Delta P)}{\Delta Q} = P + Q \frac{\Delta P}{\Delta Q}$$

### Reading 15: The firm & Market Structures

$$1. \text{ In perfect competition, Marginal revenue} = \text{Avg. Revenue} = \text{Price} = \text{Demand}$$

$$2. \text{ Marginal Revenue} = \text{Price} \times \left( 1 - \frac{1}{\text{Price Elasticity of Demand}} \right)$$

$$3. \text{ Concentration Ratio} = \frac{\text{Sum of sales values of the largest 10 firms}}{\text{Total Market Sales}}$$

$$4. \text{ Herfindahl-Hirshman Index} = \text{Sum of the squares of the market shares of the top N companies in an industry}$$

### Reading 16: Aggregate Output, Prices & Economic Growth

$$1. \text{ Nominal GDP}_t = \text{Prices in year } t \times \text{Quantity produced in year } t$$

$$2. \text{ Real GDP}_t = \text{Prices in the base year} \times \text{Quantity produced in year } t$$

$$3. \text{ Implicit price deflator for GDP or GDP deflator} = \frac{\text{value of current yr output at current yr prices}}{\text{value of current yr output at base yr prices}} \times 100$$

$$4. \text{ Real GDP} = [(\text{Nominal GDP} / \text{GDP deflator}) \div 100]$$

$$5. \text{ GDP deflator} = \frac{\text{Nominal GDP}}{\text{Real GDP}} \times 100$$

$$6. \text{ GDP} = \text{Consumer spending on final good \& services} + \text{Gross private domestic invst} + \text{Govt. spending on final goods \& services} + \text{Govt. gross fixed invst} + \text{Exp} - \text{Imp} + \text{Statistical discrepancy}$$

$$7. \text{ Net Taxes} = \text{Taxes} - \text{Transfer payments}$$

$$8. \text{ GDP} = \text{National income} + \text{Capital consumption allowance} + \text{Statistical discrepancy}$$

$$9. \text{ National Income} = \text{Compensation of employees} + \text{Corp \& Govt enterprise profits before taxes} + \text{Interest income} + \text{unincorporated business net income} + \text{rent} + \text{indirect business taxes less subsidies}$$

$$10. \text{ Total Amount Earned by Capital} = \text{Profit} + \text{Capital Consumption Allowance}$$

$$11. \text{ PI} = \text{National income} - \text{Indirect business taxes} - \text{Corp income taxes} - \text{Undistributed Corp profits} + \text{Transfer payments}$$

$$12. \text{ Personal disposable income (PDI)} = \text{Personal income} - \text{Personal taxes} \text{ OR } \text{GDP (Y)} + \text{Transfer payments (F)} - (\text{R/E} + \text{Depreciation}) - \text{direct and indirect taxes (R)}$$

$$13. \text{ Business Saving} = \text{R/E} + \text{Depreciation}$$

$$14. \text{ Household saving} = \text{PDI} - \text{Consumption expenditures} - \text{Interest paid by consumers to business} - \text{Personal transfer payments to foreigners}$$

$$15. \text{ Business sector saving} = \text{Undistributed corporate profits} + \text{Capital consumption allowance}$$